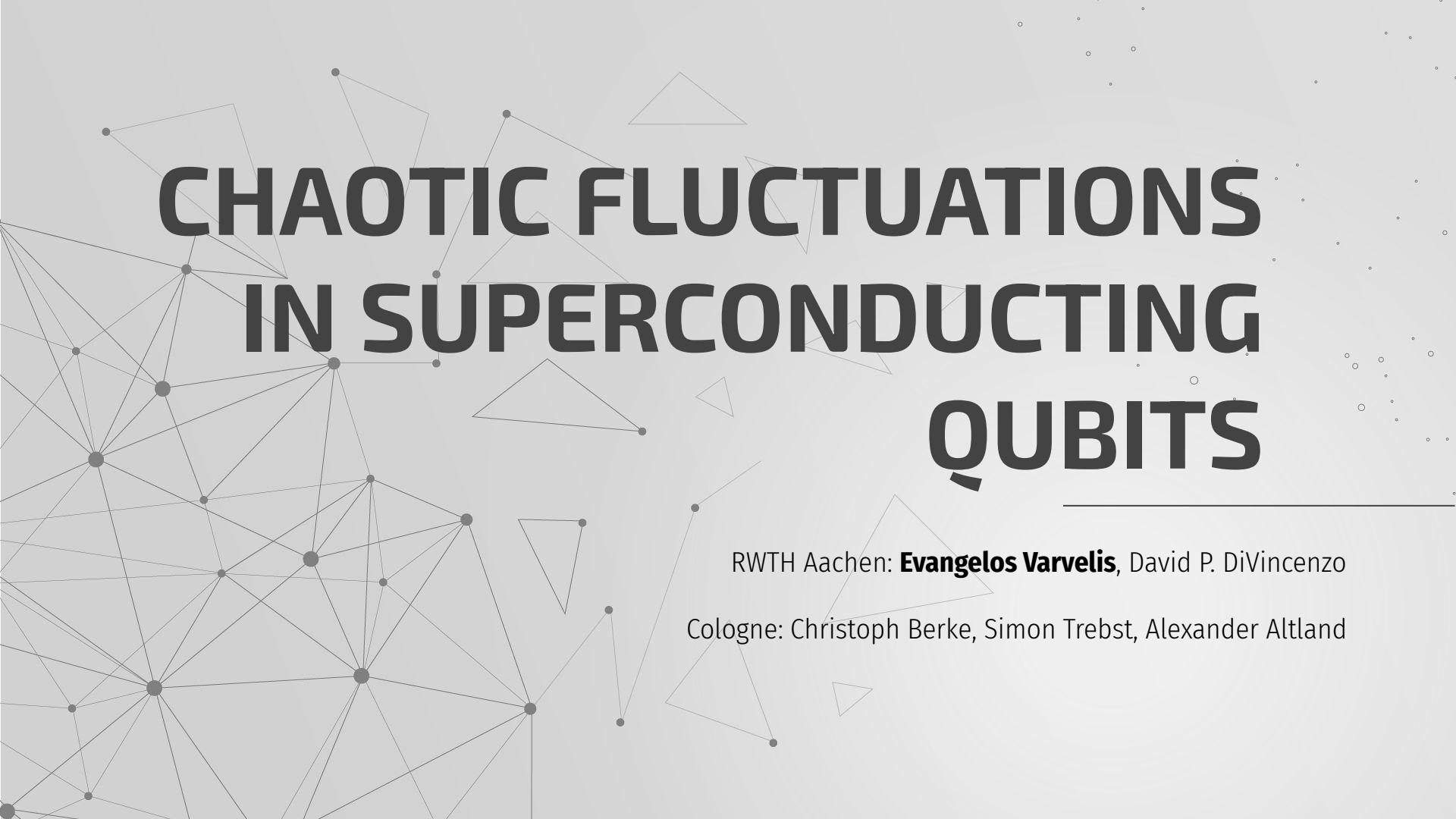


# CHAOTIC FLUCTUATIONS IN SUPERCONDUCTING QUBITS

The background features a complex network of dark grey dots connected by thin grey lines, forming a web-like structure. Scattered throughout the space are several white triangles of varying sizes, some overlapping the network and others existing independently.

RWTH Aachen: **Evangelos Varvelis**, David P. DiVincenzo

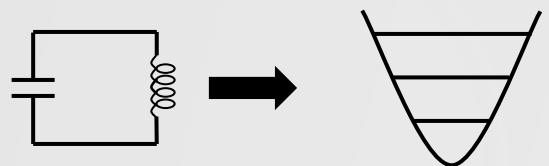
Cologne: Christoph Berke, Simon Trebst, Alexander Altland

# SUPERCONDUCTING QUBITS

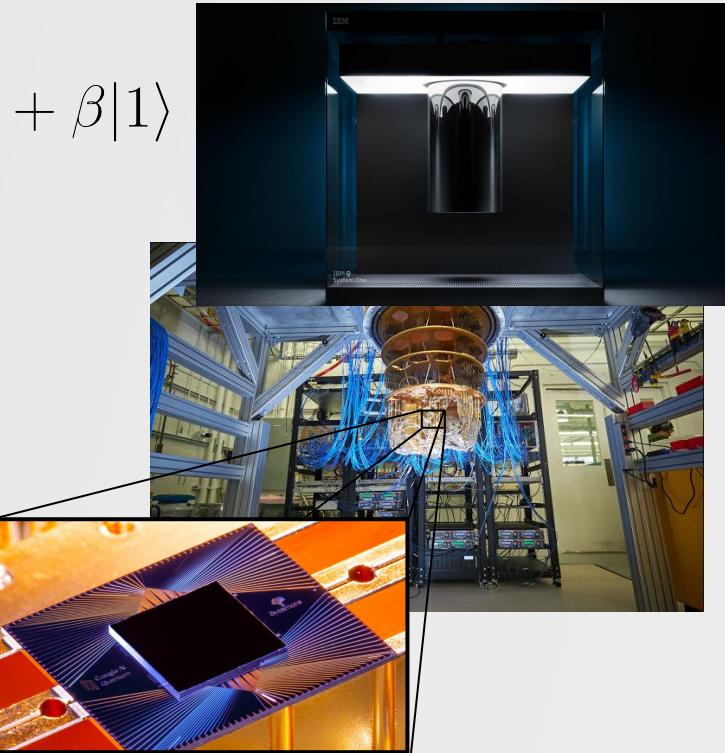
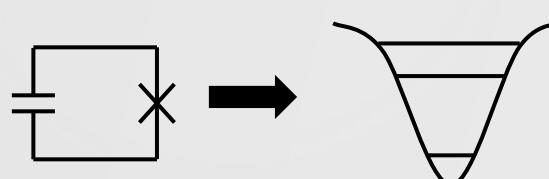
IBM's System One

Qubits:  $|\psi\rangle = \alpha| \uparrow \rangle + \beta| \downarrow \rangle \rightarrow |\psi\rangle = \alpha|0\rangle + \beta|1\rangle$

Harmonic Oscillator:  
(Bad Qubits)

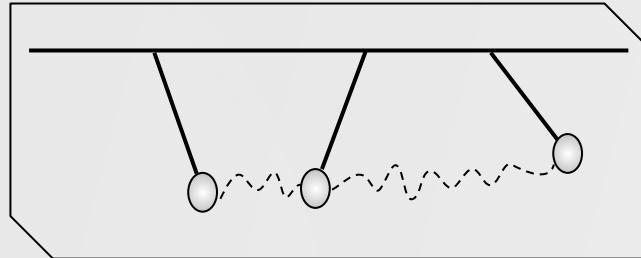
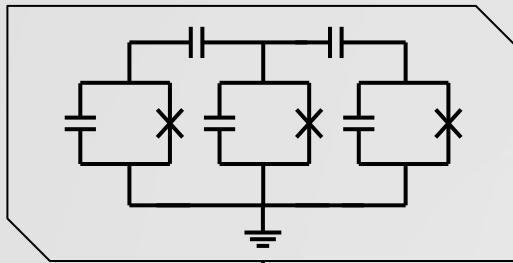


Anharmonic Oscillator:  
(Good Qubits)



Google's Sycamore Quantum Processor

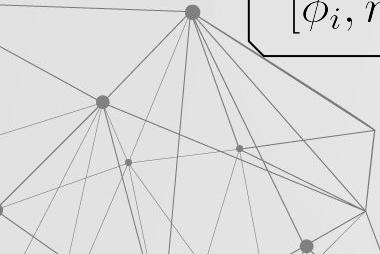
# SUPERCONDUCTING CHIPS



$$H = 4E_C \sum_{i=1}^L n_i^2 - \sum_{i=1}^L E_{J_i} \cos \phi_i + T \sum_{i=1}^{L-1} n_i n_{i+1}$$

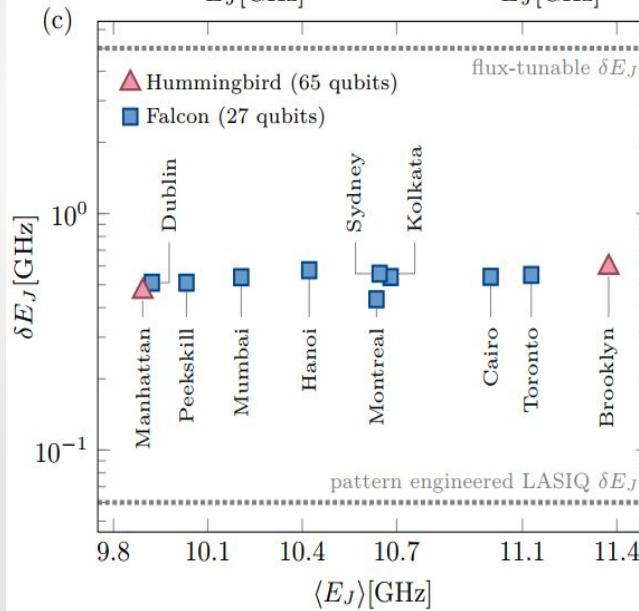
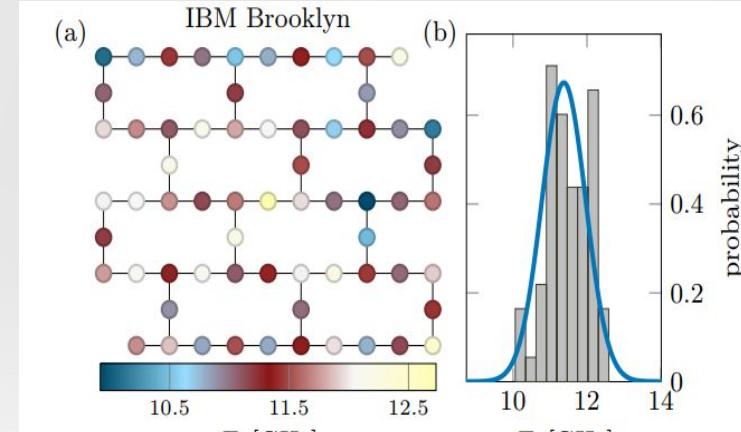
$$[\phi_i, n_j] = i\delta_{ij}$$

$$[x_i, p_j] = i\delta_{ij}$$



# JOSEPHSON ENERGY DISORDER

$$H = 4E_C \sum_{i=1}^L n_i^2 - \sum_{i=1}^L E_{J_i} \cos \phi_i + T \sum_{i=1}^{L-1} n_i n_{i+1}$$



# JOSEPHSON ENERGY DISORDER

$$H = 4E_C \sum_{i=1}^L n_i^2 - \sum_{i=1}^L E_{J_i} \cos \phi_i + T \sum_{i=1}^{L-1} n_i n_{i+1}$$

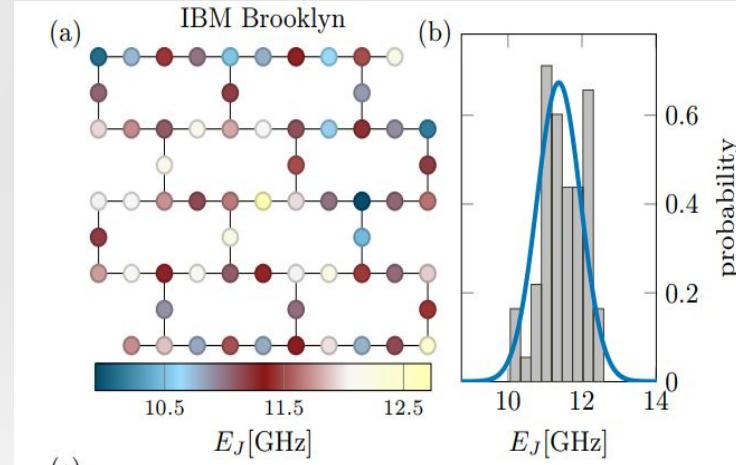


$$E_{J_i} = \langle E_J \rangle + \delta_i$$



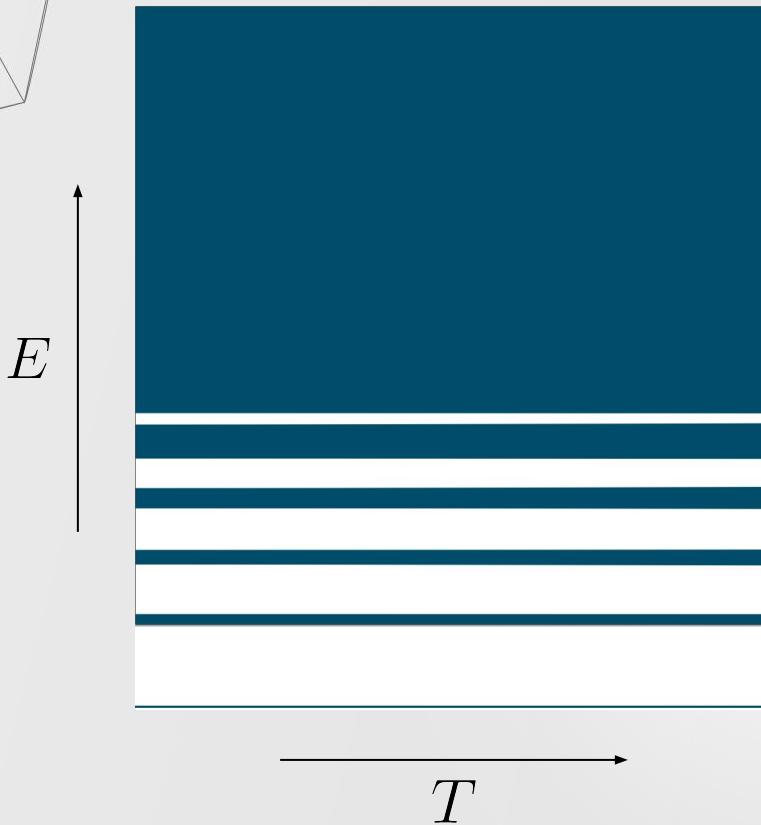
Transmon Regime  
 $E_C/\langle E_J \rangle \ll 1$

$$\delta E_J = \sqrt{\langle \delta^2 \rangle}$$

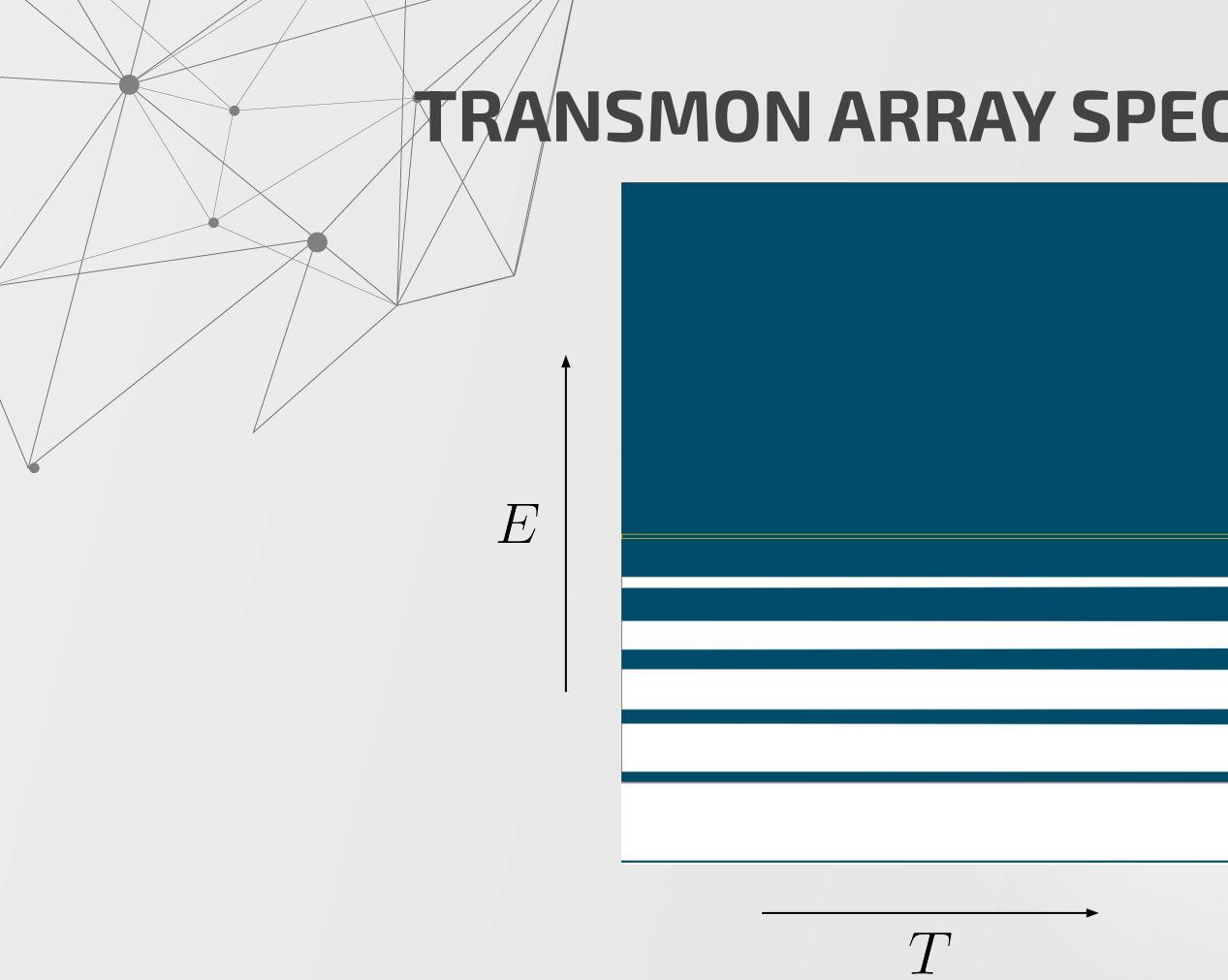




# TRANSMON ARRAY SPECTRUM



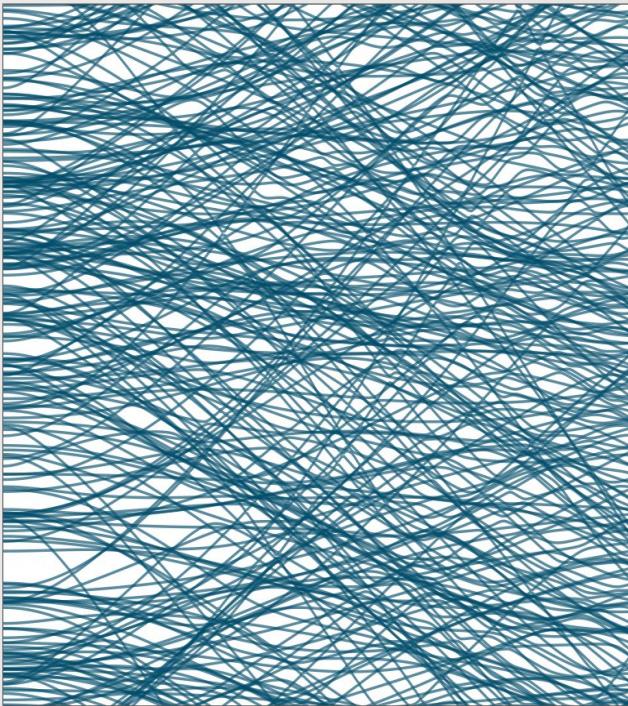
# TRANSMON ARRAY SPECTRUM





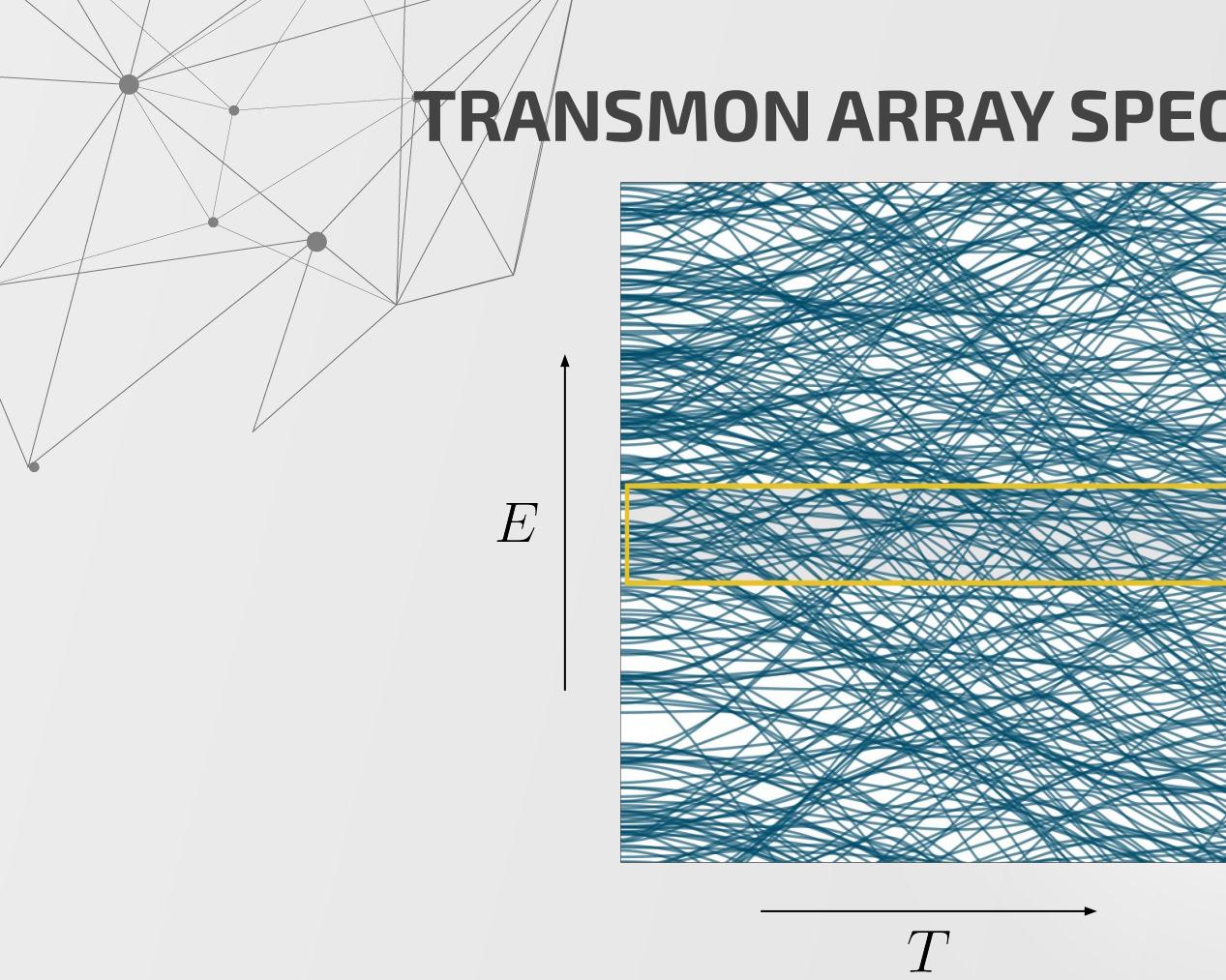
# TRANSMON ARRAY SPECTRUM

$E$



$T$

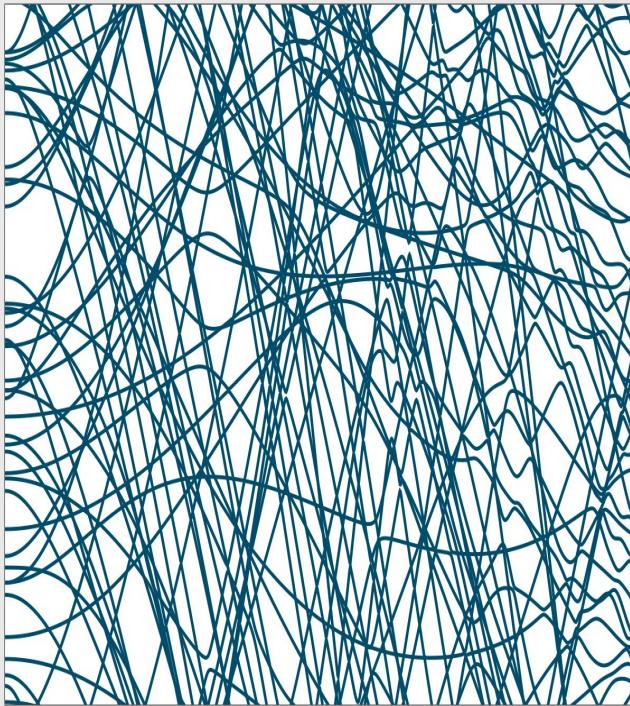
# TRANSMON ARRAY SPECTRUM





# TRANSMON ARRAY SPECTRUM

$E$

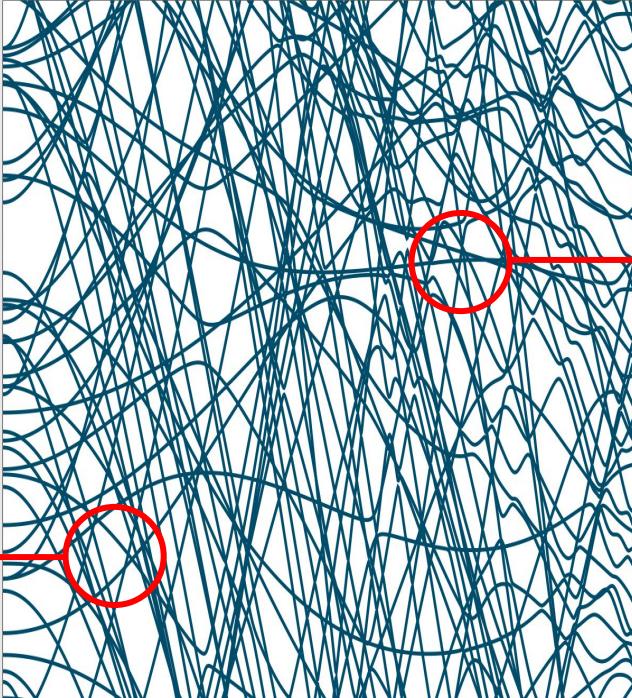


—  $T$  —

# PHASE TRANSITION



Uncorrelated (Poisson)



Scale Invariant

Logarithmic Entanglement Lightcone

Multifractal Eigenstates??



Level Repulsion (Wigner)

Quantum Chaotic

Volumic Scaling

Ballistic Entanglement Lightcone

# PHASE TRANSITION

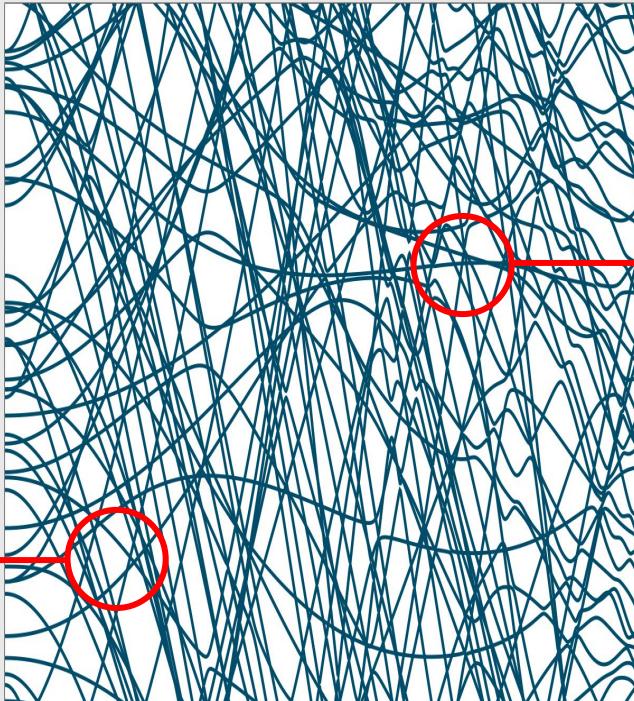


Uncorrelated (Poisson)

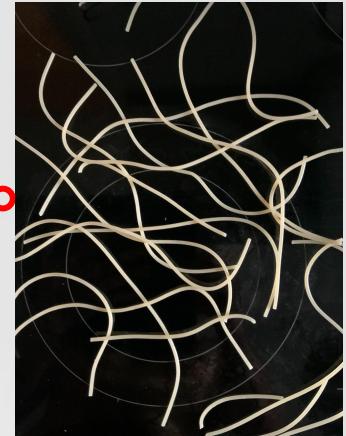
Many Body Localised

Scale Invariant

Logarithmic  
Entanglement  
Lightcone



Multifractal Eigenstates??



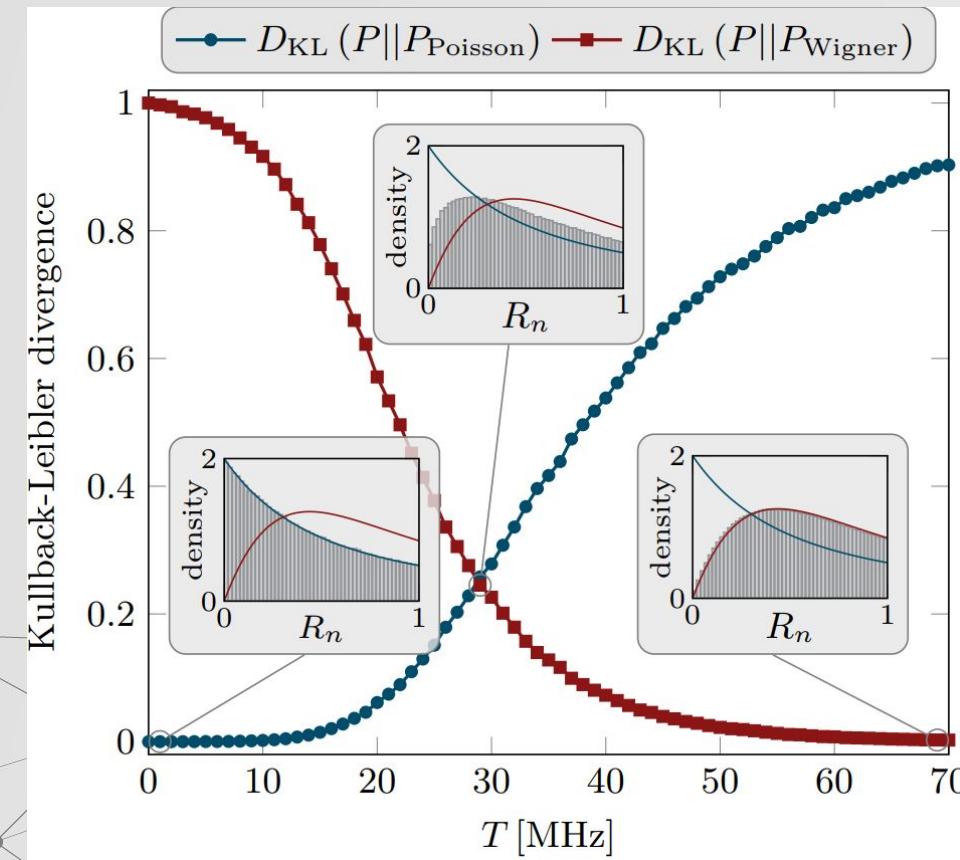
Level Repulsion (Wigner)

Quantum Chaotic

Volumic  
Scaling

Ballistic  
Entanglement  
Lightcone

# SPECTRAL STATISTICS



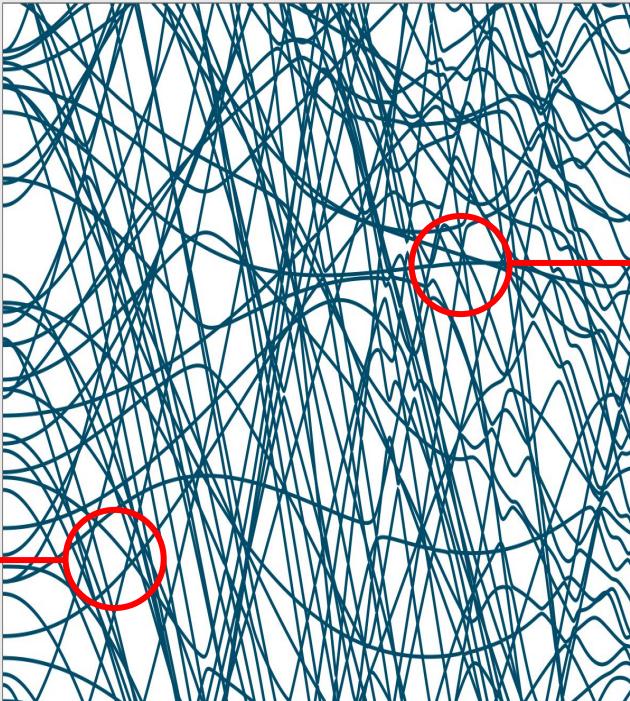
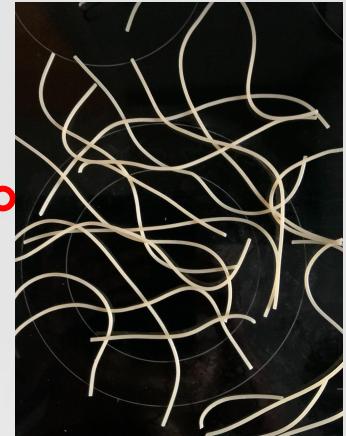
Adjacent Level Spacing Ratio

$$R_n = \min \left( \frac{E_n - E_{n-1}}{E_{n+1} - E_n}, \frac{E_{n+1} - E_n}{E_n - E_{n-1}} \right)$$

Kullback-Leibler Divergence

$$D_{\text{KL}}(P|Q) = \sum_k p_k \log \left( \frac{p_k}{q_k} \right)$$

# PHASE TRANSITION



Uncorrelated (Poisson)



Many Body Localised



**Scale Invariant**

Logarithmic Entanglement Lightcone

Level Repulsion (Wigner)



Quantum Chaotic

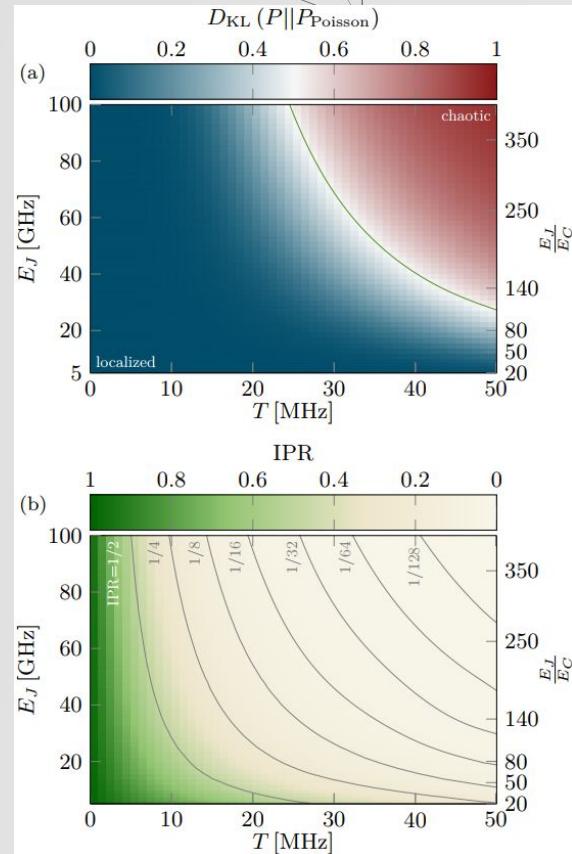
**Volumic Scaling**

Ballistic Entanglement Lightcone



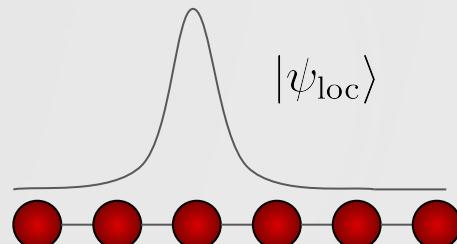
Multifractal Eigenstates??

# WAVEFUNCTION STATISTICS

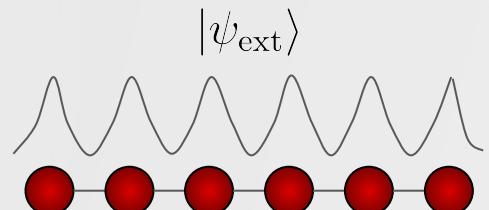


Inverse Participation Ratio

$$\text{IPR}(|\psi\rangle) = \int_0^L dx |\langle x|\psi\rangle|^4$$

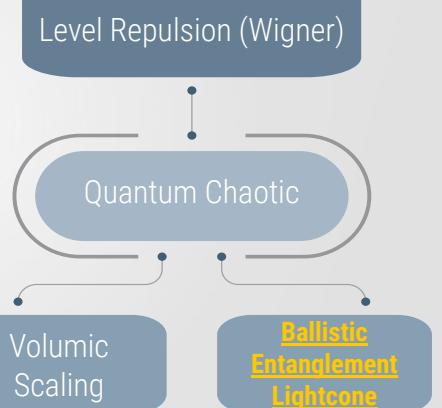
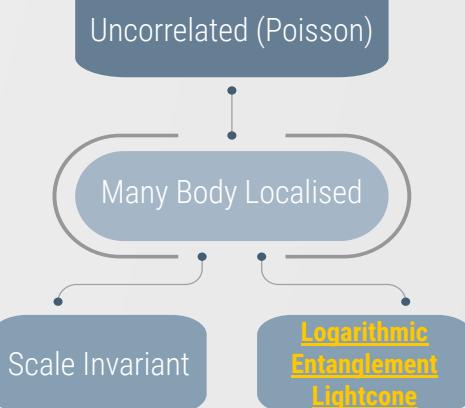
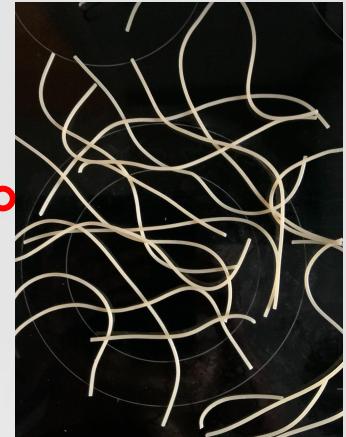
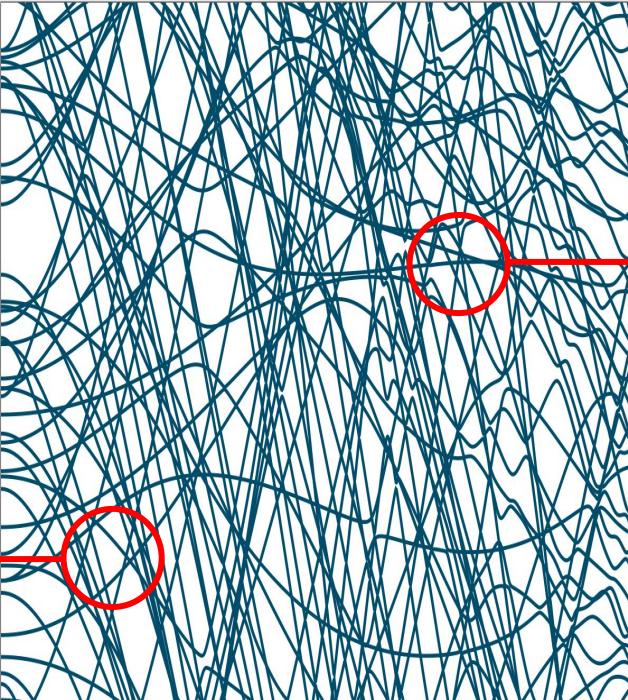


$$\text{IPR}(|\psi_{\text{loc}}\rangle) \approx 1$$



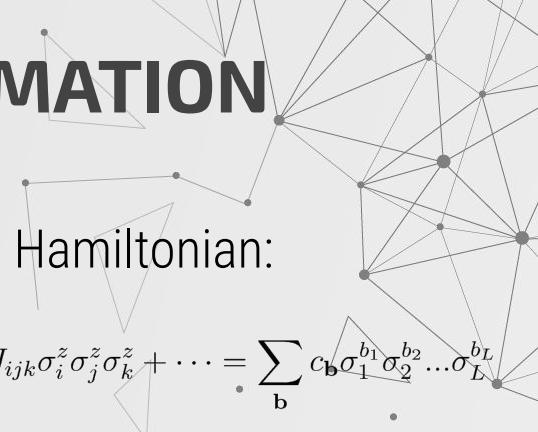
$$\text{IPR}(|\psi_{\text{ext}}\rangle) \approx \frac{1}{L}$$

# PHASE TRANSITION



Multifractal Eigenstates??

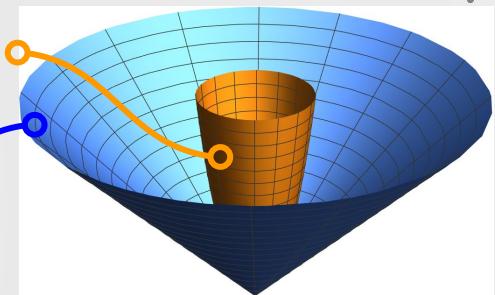
# WALSH-HADAMARD TRANSFORMATION



Local Integrals of Motion Hamiltonian:

$$H = \sum_i \omega_i \sigma_i^z + \sum_{i < j} J_{ij} \sigma_i^z \sigma_j^z + \sum_{i < j < k} J_{ijk} \sigma_i^z \sigma_j^z \sigma_k^z + \dots = \sum_{\mathbf{b}} c_{\mathbf{b}} \sigma_1^{b_1} \sigma_2^{b_2} \dots \sigma_L^{b_L}$$

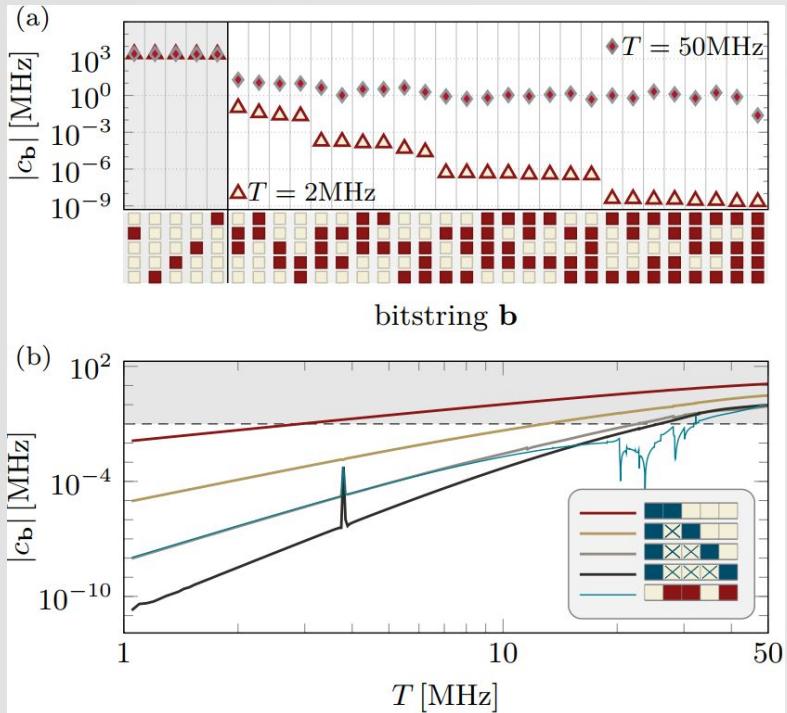
$$J_{ij} \propto e^{-(j-i)/\xi}, \quad J_{ijk} \propto e^{-(k-i)/\xi}, \quad \dots$$

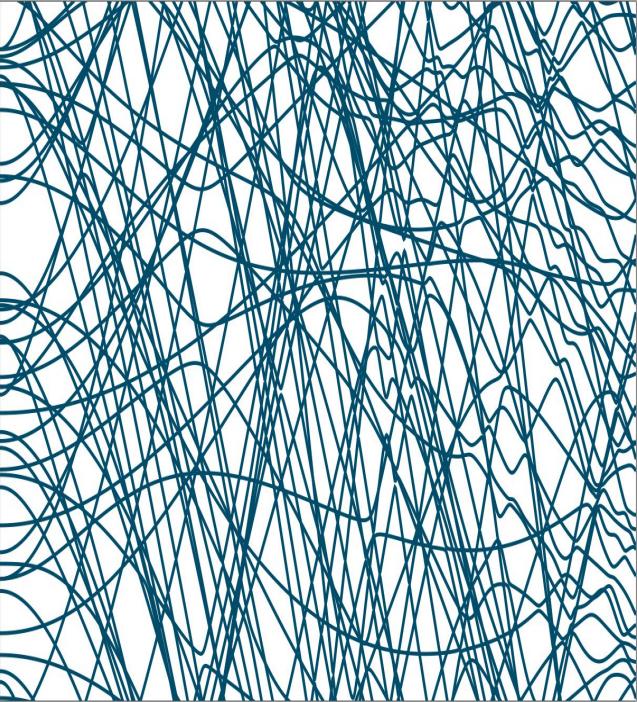


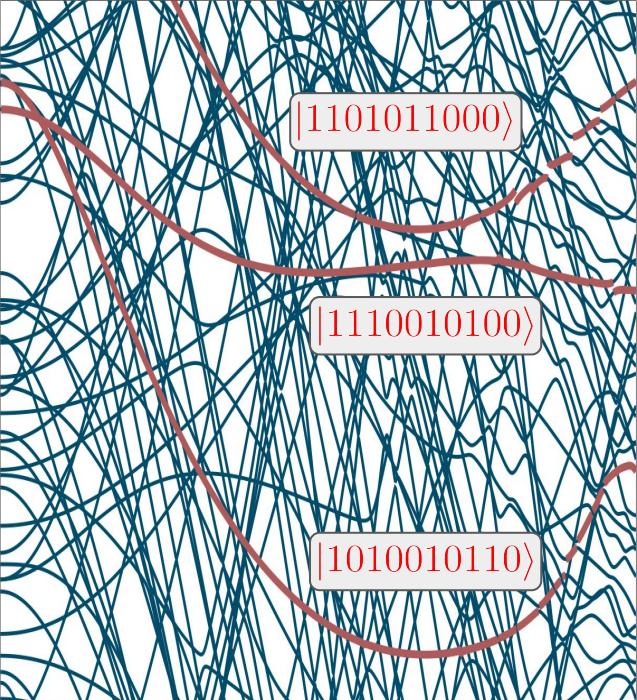
$$J_{ij\dots} = O(1)$$

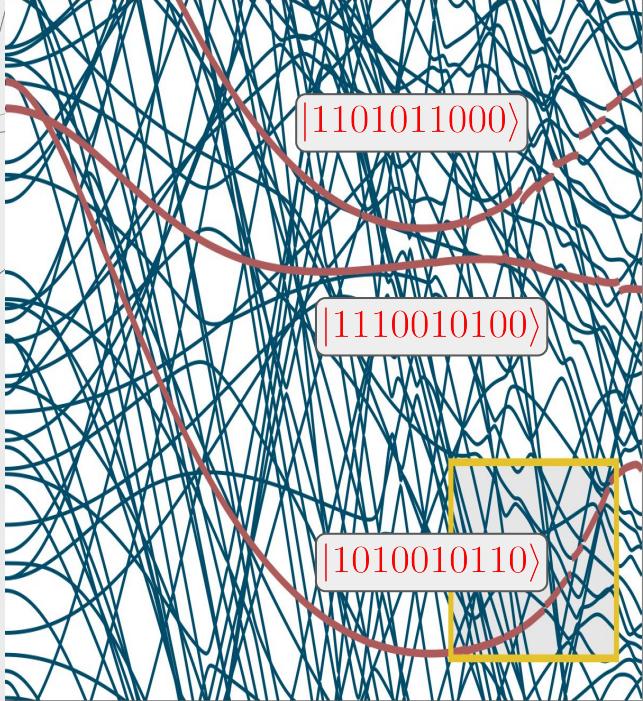
Walsh-Hadamard Transform

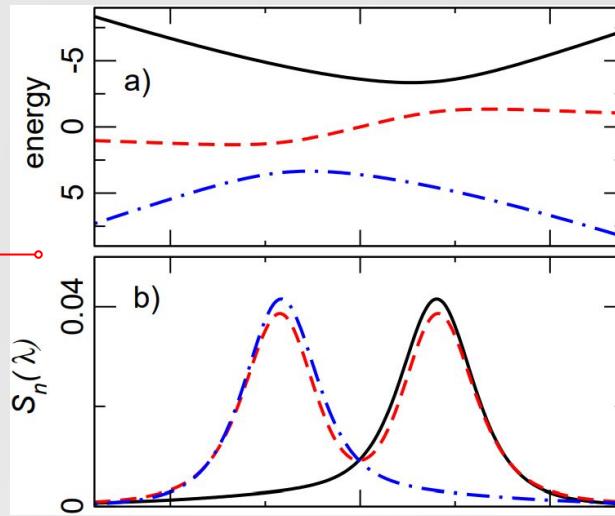
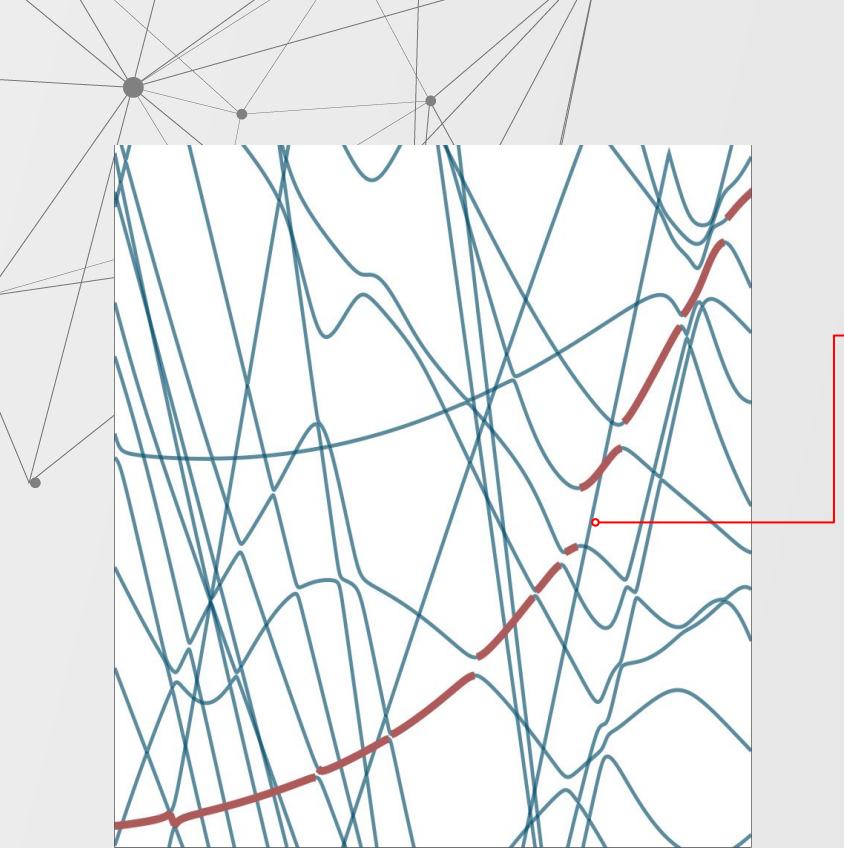
$$c_{\mathbf{b}}(T) = \frac{1}{2^L} \sum_{\mathbf{b}'} (-1)^{b_1 b'_1} (-1)^{b_2 b'_2} \dots (-1)^{b_L b'_L} E_{\mathbf{b}'}(T) = \frac{1}{2^L} \sum_{\mathbf{b}'} (-1)^{\mathbf{b} \cdot \mathbf{b}'} E_{\mathbf{b}'}(T)$$











## Eigenstate Infidelity

$$S_n(\lambda) = \frac{1 - |\langle \psi_n(\lambda + \delta\lambda) | \psi_n(\lambda) \rangle|^2}{(\delta\lambda)^2}$$



---

# THANK YOU FOR YOUR ATTENTION!!

---

Questions?

[evangelos.varvelis@rwth-aachen.de](mailto:evangelos.varvelis@rwth-aachen.de)  
arXiv:2012.05923